

INDE 301

Engineering Economy

Depreciation Methods

- 1. Understand basic terms of asset depreciation**
- 2. Apply straight line method of depreciation**
- 3. Apply DB and DDB methods of depreciation; switch between DDB and SL methods**
- 4. Explain depletion and apply cost depletion & percentage depletion methods**

Depreciation Terminology

Definition: *Book (noncash) method* to represent decrease in value of a tangible asset over time

Two types: book depreciation and tax depreciation

Book depreciation: used for *internal accounting* to track value of assets

Tax depreciation: used to determine *taxes due* based on tax laws

Common Depreciation Terms

First cost P or unadjusted basis B : Total installed cost of asset

Book value BV_t : Remaining undepreciated capital investment in year t

Recovery period n : Depreciable life of asset in years

Market value MV : Amount realizable if asset were sold on open market

Salvage value S : Estimated trade-in or MV at end of asset's useful life

Depreciation rate d_t : Fraction of first cost or basis removed each year t

Personal property: Possessions of company used to conduct business

Real property: Real estate and all improvements (land is not depreciable)

Half-year convention: Assumes assets are placed in service in midyear

Straight Line Depreciation

→ Book value decreases *linearly with time*

$$D_t = \frac{B - S}{n}$$

Where: D_t = annual depreciation charge
 t = year

B = first cost or unadjusted basis

S = salvage value

n = recovery period

$$BV_t = B - tD_t$$

Where: BV_t = book value after t years

SL depreciation rate is **constant** for each year: $d = d_t = 1/n$

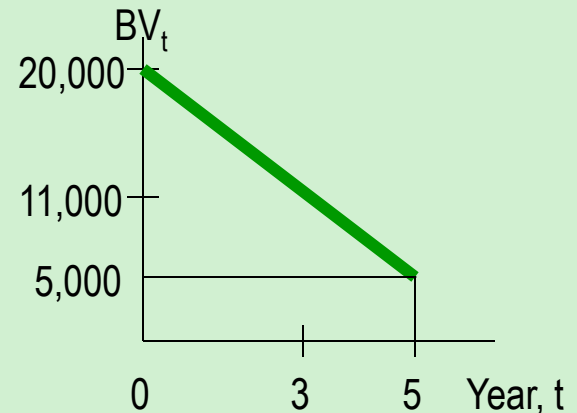
Example: SL Depreciation

An argon gas processor has a first cost of \$20,000 with a \$5,000 salvage value after 5 years. Find (a) D_3 and (b) BV_3 for year three. (c) Plot book value vs. time.

Solution: (a) $D_3 = (B - S)/n$
 $= (20,000 - 5,000)/5$
 $= \$3,000$

(b) $BV_3 = B - tD_t$
 $= 20,000 - 3(3,000)$
 $= \$11,000$

(c) Plot BV vs. time



Declining Balance (DB) and Double Declining Balance (DDB) Depreciation

→ Determined by multiplying BV at beginning of year by fixed percentage d



Max rate for d is twice straight line rate, i.e., $d \leq 2/n$

Cannot depreciate below salvage value

Depreciation for year t is obtained by either relation:

$$D_t = dB(1 - d)^{t-1} = dBV_{t-1}$$

Where: D_t = depreciation for year t

d = uniform depreciation rate ($2/n$ for DDB)

B = first cost or unadjusted basis

BV_{t-1} = book value at end of previous year

Book value for year t is given by:

$$BV_t = B(1 - d)^t$$

Example: Double Declining Balance

A depreciable construction truck has a first cost of \$20,000 with a \$4,000 salvage value after 5 years. Find the (a) depreciation, and (b) book value after 3 years using DDB depreciation.

Solution:

$$(a) \quad d = 2/n = 2/5 = 0.4$$

$$\begin{aligned} D_3 &= dB(1 - d)^{t-1} \\ &= 0.4(20,000)(1 - 0.40)^{3-1} \\ &= \$2880 \end{aligned}$$

$$\begin{aligned} (b) \quad BV_3 &= B(1 - d)^t \\ &= 20,000(1 - 0.4)^3 \\ &= \$4320 \end{aligned}$$

Spreadsheet Functions for Depreciation

Straight line function: $\text{SLN}(B, S, n)$

Declining balance function: $\text{DB}(B, S, n, t)$

Double declining balance function: $\text{DDB}(B, S, n, t, d)$

Note: It is better to use the DDB function for DB and DDB depreciation. DDB function checks for $BV < S$ and is more accurate than the DB function.

Depletion Methods

Depletion: book (noncash) method to represent decreasing value of *natural resources*

★ **Two methods:** *cost* depletion (CD) and *percentage* depletion (PD) ★

Cost depletion: Based on level of activity to remove a natural resource

➤ Calculation: Multiply factor CD_t by amount of resource removed

Where: $CD_t = \text{first cost} / \text{resource capacity}$

➤ Total depletion can not exceed first cost of the resource

Percentage depletion: Based on gross income (GI) from resource

➤ Calculation: Multiply GI by standardized rate (%) from table

➤ Annual depletion can not exceed 50% of company's taxable income (TI)

Example: Cost and Percentage Depletion

A mine purchased for \$3.5 million has a total expected yield of one million ounces of silver. Determine the depletion charge in year 4 when 300,000 ounces are mined and sold for \$30 per ounce using (a) cost depletion, and (b) percentage depletion. (c) Which is larger for year 4?

Solution: Let depletion amounts equal CDA_4 and PDA_4

(a) Factor, $CD_4 = 3,500,000 / 1,000,000 = \3.50 per ounce

$$CDA_4 = 3.50(300,000) = \$1,050,000$$

(b) Percentage depletion rate for silver mines is 0.15

$$PDA_4 = (0.15)(300,000)(30) = \$1,350,000$$

(c) Claim **percentage depletion** amount, provided it is $\leq 50\%$ of TI